Multi-Task Learning from Large-Scale High-Dimensional Data

(joint work with Patrick Simianer* and Chris Dyer[†])

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Introduction		Conclusion		
Big Data				

• Data can be characterized as big by

- large size of training set,
- high dimensionality of feature representation of data.
- Not all datasets advertised as "large" meet both requirements (e.g. Learning-to-Rank Challenges at Yahoo! and Microsoft work on *hundreds* of features for *tens of thousands* of queries)
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Large Scale Learning

• Learning problem is large scale if

- training data cannot be stored in RAM (Langford on http://hunch.net/?p=330, 2008),
- time constraint requires that algorithms scale at worst linearly with number of examples (Bottou & Bousquet NIPS'07).
- Solutions:
 - **Online learning** for linear scaling in training sample size (Bottou & Le Cun NIPS'04),
 - combined with **feature selection** for memory efficient feature representation (Langford et al. JMLR'09),
 - combined with parallelization and averaging for parallel acceleration and reduced variance at asymptotic online learning guarantees (Zinkevich et al. NIPS'10).
- We add another dimension: Multi-task learning.

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Multi-Task Learning

- **Goal:** A number of statistical models need to be estimated simultaneously from data belonging to different tasks.
- Examples:
 - OCR of handwritten characters from different writers: Exploit commonalities on pixel- or stroke-level shared between writers.
 - LTR from search engine query logs from different countries: Some queries are country-specific ("football"), most preference rankings are shared across countries.
- Idea:
 - Learn a shared model that takes advantage of commonalities among tasks, without neglecting individual knowledge.

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Our Application: Learning from Big Data in SMT

- Machine learning theory and practice suggests benefits from using expressive feature representations and from tuning on large training samples.
- Discriminative training in SMT has mostly been content with tuning small sets of dense features on small development data (Och NAACL'03).
- Notable exceptions using larger feature and training sets:
 - Liang et al. ACL'06: 1.5M features, 67K parallel sentences.
 - Tillmann and Zhang ACL'06: 35M feats, 230K sents.
 - Blunsom et al. ACL'08: 7.8M feats, 100K sents.
 - Simianer, Riezler, Dyer ACL'12: 4.7M feats, 1.6M sents.
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Our Approach: Multi-Task Distributed SGD

• Distribute work and share information!

- Online learning via Stochastic Gradient Descent optimization.
- Distributed learning using Hadoop/MapReduce of SunGridEngine.
- Feature selection via ℓ_1/ℓ_2 block norm regularization on features across multiple tasks.
- Pooling baseline:
 - Concatenate data from all tasks into one big pool.
 - Becomes infeasible very quickly.
- Independent modeling baseline :
 - Independent training of task specific models.
 - Does not share any knowledge across tasks.

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Related Work

• Online learning:

- We deploy pairwise ranking perceptron (Shen & Joshi JMLR'05)
- and margin perceptron (Collobert & Bengio ICML'04).

Distributed learning:

- Without feature selection, our algorithm reduces to Iterative Mixing (McDonald et al. NAACL'10),
- which itself is related to Bagging (Breiman JMLR'96) if shards are treated as random samples.

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Related Work

• l₁/l₂ regularization:

- Related to group-Lasso approaches which use mixed norms (Yuan & Lin JRSS'06), hierarchical norms (Zhao et al. Annals Stats'09), structured norms (Martins et al. EMNLP'11).
- Difference: Norms and proximity operators are applied to groups of features in single regression or classification task – multi-task learning groups features orthogonally by tasks.
- Closest relation to Obozinski et al. StatComput'10: Our algorithm is weight-based backward feature elimination variant of their gradient-based forward feature selection algorithm.

OL Framework: Pairwise Ranking Perceptron

- Preference pairs $\mathbf{x}_j = (\mathbf{x}_j^{(1)}, \mathbf{x}_j^{(2)})$ where $\mathbf{x}_j^{(1)}$ is ordered above $\mathbf{x}_j^{(2)}$ w.r.t. sentence-wise BLEU (Nakov et al. COLING'12).
- Hinge loss-type objective

 $l_j(\mathbf{w}) = (-\langle \mathbf{w}, \bar{\mathbf{x}}_j \rangle)_+$

where $\bar{\mathbf{x}}_j = \mathbf{x}_j^{(1)} - \mathbf{x}_j^{(2)}$, $(a)_+ = \max(0, a)$, $\mathbf{w} \in \mathbb{R}^D$ is a weight vector, and $\langle \cdot, \cdot \rangle$ denotes the standard vector dot product.

• Ranking perceptron by stochastic subgradient descent:

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Algorithms		Conclusion

OL framework: Margin Perceptron

Hinge loss-type objective

$$I_j(\mathbf{w}) = (1 - \langle \mathbf{w}, \bar{\mathbf{x}}_j \rangle)_+$$

• Stochastic subgradient descent:

$$abla l_j(\mathbf{w}) = egin{cases} -ar{\mathbf{x}}_j & ext{if } \langle \mathbf{w}, ar{\mathbf{x}}_j
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- Margin term controls capacity, but results in more updates.
- Collobert & Bengio (ICML'04) argue that this justifies not using an explicit regularization (as for example in an SGD version of the SVM (Shalev-Shwartz et al. ICML'07)).

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MTL Framework: ℓ_1/ℓ_2 Block Norm Regularization

Data points {(*x_{zn}*, *y_{zn}*), *z* = 1,..., *Z*, *n* = 1,..., *N_z*}, sampled from *P_z* on *X* × *Y* (*z* = task; *n* = data point).

• Objective:

 $\min_{\mathbf{W}} \sum_{z,n} I_n(\mathbf{w}_z) + \lambda \|\mathbf{W}\|_{1,2}$

 where W = (w^d_z)_{z,d} is a Z-by-D matrix W = (w^d_z)_{z,d} of D-dimensional row vectors w_z and Z-dimensional column vectors w^d of weights associated with feature d across tasks.

Weighted l₁/l₂ norm:

$$\lambda \|\mathbf{W}\|_{1,2} = \lambda \sum_{d=1}^{D} \|\mathbf{w}^{d}\|_{2}$$

 Each l₂ norm of a weight column w^d represents the relevance of the corresponding feature across tasks.

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ℓ_1/ℓ_2 Re	ℓ_1/ℓ_2 Regularization Explained														
		\mathbf{w}^1 6 0	\mathbf{w}^2	\mathbf{w}^3	\mathbf{w}^4	\mathbf{w}^5			\mathbf{w}^1	\mathbf{w}^2	\mathbf{w}^3	\mathbf{w}^4	\mathbf{w}^5		
	\mathbf{w}_{z_1} [\mathbf{w}_{z_2} [6	4	0	0	0]	[6	4	0	0	0]	
	W 22	0	0	3	0	0	1] [3	0	0	0	0	1	

- be **0** and others to have high weights across tasks.
- Algorithm idea:
 - Contribution to loss reduction must outweigh regularizer penalty in order to activate feature by non-zero weight.
 - Weight-based feature elimination criterion:

If $\|\mathbf{w}^d\|_2 \leq \lambda$, set $\mathbf{W}[z][d] = 0, \forall z$.

Implementation by threshold on K features or by threshold λ.

	Algorithm	าร											Conclusion		
ℓ_1/ℓ_2 Regularization Explained															
		\mathbf{w}^1	\mathbf{w}^2	\mathbf{w}^3	\mathbf{w}^4	\mathbf{w}^5			\mathbf{w}^1	\mathbf{w}^2	\mathbf{w}^3	\mathbf{w}^4	\mathbf{w}^5		
	\mathbf{w}_{z_1} [6	$\frac{\mathbf{w}^2}{4}$	0	0	0]	[6	4	0	0	0]	
	\mathbf{w}_{z_2} [0		3	0	0]	[3	0	0	0	0]	
	\mathbf{w}_{z_3} [0	0	0	2	3]	[2	3	0	0	0]	
colum	nn ℓ_2 norm:	6	4	3	2	3			7	5	0	0	0		
	ℓ_1 sum:					\Rightarrow	18						\Rightarrow	12	

• ℓ_1 sum of ℓ_2 norms encourages several feature columns \mathbf{w}^d to be **0** and others to have high weights across tasks.

Algorithm idea:

 ℓ_1 sum:

- Contribution to loss reduction must outweigh regularizer penalty in order to activate feature by non-zero weight.
- Weight-based feature elimination criterion:

If
$$\|\mathbf{w}^d\|_2 \leq \lambda$$
, set $\mathbf{W}[z][d] = 0, \forall z$.

Implementation by threshold on K features or by threshold λ .

Multi-Task Learning Algorithm

Algorithm 1 Multi-task Distributed SGD

```
Get data for Z tasks, each including S sentences;
distribute to machines.
Initialize \mathbf{v} \leftarrow \mathbf{0}.
for epochs t \leftarrow 0 \dots T - 1: do
for all tasks z \in \{1 \dots Z\}: parallel do
Perform task-specific learning
end for
Stack weights \mathbf{W} \leftarrow [\mathbf{w}_{1,t,S,0}| \dots |\mathbf{w}_{Z,t,S,0}]^T
Perform \ell_1/\ell_2 regularization
end for
return \mathbf{v}
```

Implementation as Feature Selection Algorithm

Algorithm 2 Multi-task Distributed SGD

```
Get data for Z tasks, each including S sentences;
distribute to machines.
Initialize \mathbf{v} \leftarrow \mathbf{0}.
for epochs t \leftarrow 0 \dots T - 1: do
     for all tasks z \in \{1 \dots Z\}: parallel do
          \mathbf{W}_{z,t,0,0} \leftarrow \mathbf{V}
          for all sentences i \in \{0 \dots S - 1\}: do
                Decode i<sup>th</sup> input with \mathbf{w}_{z,t,i,0}.
                for all pairs i \in \{0 \dots P - 1\}: do
                     \mathbf{w}_{z,t,i,i+1} \leftarrow \tilde{\mathbf{w}}_{z,t,i,i} - \eta \nabla l_i(\mathbf{w}_{z,t,i,i})
                end for
                \mathbf{W}_{z,t,i+1,0} \leftarrow \mathbf{W}_{z,t,i,P}
          end for
     end for
     Stack weights \mathbf{W} \leftarrow [\mathbf{w}_{1,t,S,0}] \dots |\mathbf{w}_{Z,t,S,0}|^T
     Select top K feature columns of W by \ell_2 norm
     for k \leftarrow 1 \dots K do
          \mathbf{v}[k] = \frac{1}{Z} \sum_{\tau=1}^{Z} \mathbf{W}[z][k]
     end for
end for
return v
```

Implementation as Adaptive Path-Following Algorithm

Algorithm 3 Path-Following Multi-task Distributed SGD

```
Get data for Z tasks, each including S sentences; distribute to machines.
Initialize \mathbf{v} \leftarrow \mathbf{0}; \lambda_0, \lambda_{\min}, \epsilon.
for epochs t \leftarrow 0 \dots T - 1: do
     for all tasks z \in \{1 \dots Z\}: parallel do
           Perform task-specific learning
     end for
     Stack weights \mathbf{W} \leftarrow [\mathbf{w}_{1,t,S,0}| \dots |\mathbf{w}_{Z,t,S,0}]^T
     for feature columns d \in \{1 \dots D\} in W: do
          if \|\mathbf{w}^d\|_2 \leq \lambda_t then
               v[\ddot{d}] = 0
          else
               \mathbf{v}[d] = \frac{1}{Z} \sum_{i=1}^{Z} \mathbf{W}[z][d]
          end if
     end for
     Set \lambda_{t+1} = \min\{\lambda_t, \frac{\sum_{z,i,j}(l_{z,i,j}(\mathbf{v}_{t-1}) - l_{z,i,j}(\mathbf{v}_t))}{2}\}
     if \lambda_{t+1} < \lambda_{\min} then
           break
     end if
end for
return v
```

SMT using Synchronous Context-Free Grammars

- (1) $X \to X_1$ hat X_2 versprochen; X_1 promised X_2 (2) $X \to X_1$ hat mir X_2 versprochen;
- (3) $X \rightarrow X_1$ versprach X_2 ; X_1 promised X_2
- Hierarchical phrase-based translation (Chiang CL'07), formalizes translation rules as productions of synchronous context-free grammar (SCFG).
- Features in discriminative training:
 - **Rule identifiers** for SCFG productions Examples: rule (1), (2) and (3)
 - Rule n-gram features in source and target Examples: "X hat", "hat X", "X versprochen"
 - Rule shape features
 Examples: (NT, term*, NT, term*; NT, term*, NT) for (1), (NT, term*, NT; NT, term*, NT) for rule (3).

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- (1) $X \rightarrow X_1$ hat X_2 versprochen; X_1 promised X_2
- (2) $X \rightarrow X_1$ hat mir X_2 versprochen;
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 $\begin{array}{l} \mbox{Examples: (NT, term*, NT, term*; NT, term*, NT) for (1), (2); \\ (NT, term*, NT; NT, term*, NT) for rule (3). \end{array}$

Experiment I: Random Sharding on Large Parallel Data

- **Idea:** Take advantage of inherent efficiency (and effectiveness) of multi-task learning.
 - Define tasks as random shards of data,
 - either by sharding once or by re-sharding after each epoch.
- Advantage:
 - Hadoop/MapReduce framework offers parallelization by data sharding.
 - Feature selection by ℓ_1/ℓ_2 block norm regularization on shards iteratively cuts feature space to feasible size.
- See Simianer, Riezler, Dyer ACL'12.

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	Random Sharding	Conclusion

Data

News Commentary(nc)

	train-nc	lm-train- <i>nc</i>	dev-nc	devtest-nc	test-nc
Sentences	132,753	180,657	1057	1064	2007
Tokens de	3,530,907	—	27,782	28,415	53,989
Tokens en	3,293,363	4,394,428	26,098	26,219	50,443
Rule Count	14,350,552 (1G)	-	2,322,912	2,320,264	3,274,771

$\operatorname{Europarl}(ep)$

	$\operatorname{train-}ep$	$\operatorname{lm-train-}ep$	$\operatorname{dev-}ep$	devtest-ep	$ ext{test-}ep$
Sentences	1,655,238	2,015,440	2000	2000	2000
Tokens de	45,293,925	—	57,723	56,783	59,297
Tokens en	45,374,649	54,728,786	58,825	58,100	60,240
Rule Count	203,552,525 (31.5G)	_	17,738,763	$17,\!682,\!176$	$18,\!273,\!078$

News Crawl(crawl)

	dev-crawl	test-crawl10	test-crawl11
Sentences	2051	2489	3003
Tokens de	49,848	64,301	76,193
Tokens en	49,767	61,925	74,753
Rule Count	9,404,339	11,307,304	$12,\!561,\!636$

		Random Sharding	Conclusion
SMT Setup)		

- cdec (Dyer et al. ACL'10) framework for decoding and induction of SCFGs.
- SCFG per-sentence grammars are stored on disk instead of in memory (Lopez EMNLP'07), extracted by leave-one-out (Zollmann and Sima'an JACL'05) for training-set tuning.
- Scale:
 - Data are split into shards holding about 1,000 sentences, corresponding to dev set size.
 - On Hadoop/MapReduce cluster for 300 parallel jobs this required 2,290 shards for *ep* data set.
 - 5M active features without feature selection on ep data set.

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Results on News Commentary (nc) data

Algorithm	Tuning set	Features	#Features	test-nc
Single-task SGD	dev- <i>nc</i>	default	12	28.0
	dev-nc	+id,ng,shape	180k	28.15
Multi-task SGD	train- <i>nc</i>	+id,ng,shape	100k	28.81

- Scaling from 12 to 180K features on dev set does not help.
- Scaling to full feature- and training-set does help (+0.8 BLEU).
- Statistical significance assessed by Approximate Randomization (Noreen'89).

Results on Europarl (ep) and News Crawl (crawl) data

Algorithm	Tuning set	Features	#Features	test- <i>ep</i>
Single-task SGD	dev- <i>ep</i>	default	12	26.42
	dev- <i>ep</i>	+id,ng,shape	300k	28.37
Multi-task SGD	train- <i>ep</i>	+id,ng,shape	100k	28.62

Alg.	Tuning set	Features	#Feats	test- <i>crawl</i> 10	test- <i>crawl</i> 11
ST	dev- <i>crawl</i> dev- <i>crawl</i>	default +id,ng,shape	12 300k	15.39 17.8	14.43 16.83
MT	train- <i>ep</i>	+id,ng,shape	100k	19.12	17.33

- Scaling up feature sets helps even for dev-set tuning.
- On large scale tuning set only Multi-task SGD is feasible.
- Additional gains of 0.5 to 1.3 BLEU by scaling to large tuning set on out-of-domain news crawl test data.

Experiments II: Random vs. Natural Tasks

Research Question:

- As shown, multi-task learning can be used as general regularization technique on random shards.
- Can multi-task learning benefit from natural task structure in the data, where shared and individual knowledge is properly balanced?
- See Simianer & Riezler WMT'13.

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			Natural Tasks	Conclusion
Data				
	AB	Human Necessities Performing Operations, Transportir	ng	

- C Chemistry, Metallurgy
- D Textiles, Paper
- E Fixed Constructions
- F Mechanical Engineering, Lighting, Heating, Weapons
- G Physics
- H Electricity
- International Patent Classification (IPC) categorizes patents hierarchically into eight sections, 120 classes, 600 subclasses, down to 70,000 subgroups at the leaf level.
- Typically, a patent belongs to more than one section, with one section chosen as main classification.
- Eight top classes/sections used to define **natural tasks**.

SMT and Learning Setup

- SCFG framework using sparse local features (as above).
- Learning algorithms:
 - Baselines:
 - MERT (Kumar et al. ACL'09)
 - Single-task perceptron w/ and w/o ℓ_1 regularization with clipping (Carpenter 2008)
 - Single-task margin perceptron (Collobert & Bengio ICML'04).
 - Multi-task tuning using standard and margin perceptron.
 - Tuning methods with random components (MERT, random (re)sharding) were repeated 3 times and BLEU scores averaged.

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Train/dev/test splits

• 1.2M parallel sentences from patent domain for training¹.

- Development and test sets of 2,000 sentences from each of sections A to H for **independent** tuning and testing.
- **Pooled** development and test sets containing 2,000 sentences with all sections evenly represented.
- Pooled-cat development set for tuning on concatenation of data from all sections.

¹http://www.cl.uni-heidelberg.de/statnlpgroup/pattr

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MERT Baseline w/ 12 Dense Features

	single-task tuning			
	indep. ⁰	pooled 1	pooled-cat ²	
pooled test	-	51.18	51.22	
А	54.92	⁰² 55.27	⁰ 55.17	
В	51.53	51.48	⁰¹ 51.69	
С	¹² 56.31	² 55.90	55.74	
D	49.94	⁰ 50.33	⁰ 50.26	
Е	¹ 49.19	48.97	¹ 49.13	
F	¹² 51.26	51.02	51.12	
G	¹ 49.61	49.44	49.55	
Н	49.38	49.50	⁰¹ 49.67	
average test	51.52	51.49	51.54	

- Neither tuning on *pooled* or *pooled-cat* improves over *indep*..
- $x \in \{0,1,2\}$ BLEU denotes statistical significance of pairwise test.

Single-Task Perceptron w/ ℓ_1 Regularization

	single-task tuning				
	indep. ⁰	pooled 1	pooled-cat ²		
pooled test	-	50.75	¹ 52.08		
А	¹ 55.11	54.32	⁰¹ 55.94		
В	¹ 52.61	50.84	¹ 52.57		
С	56.18	56.11	⁰¹ 56.75		
D	¹ 50.68	49.48	⁰¹ 51.22		
Е	¹ 50.27	48.69	¹ 50.01		
F	¹ 51.68	50.71	¹ 51.95		
G	¹ 49.90	49.06	⁰¹ 50.51		
Н	¹ 50.48	49.16	¹ 50.53		
average test	52.11	51.05	52.44		
model size	430,092.5	457,428	1,574,259		

- Improvements over MERT, mostly on pooled-cat tuning set.
- 1.5M features make serial tuning on *pooled-cat* infeasible.
- Overfitting effect on small *pooled* data.

Single- and Multi-Task Perceptron

	single-task tuning			n	nulti-task tuni	ng
	indep. ⁰	pooled ¹	pooled-cat ²	IPC ³	sharding 4	resharding 5
pooled test	-	51.33	1 51.77	¹² 52.56	¹² 52.54	¹² 52.60
A	54.79	54.76	⁰¹ 55.31	012 56.35	012 56.22	012 56.21
В	¹² 52.45	51.30	¹ 52.19	⁰¹² 52.78	0123 52.98	⁰¹² 52.96
С	² 56.62	56.65	1 56.12	⁰¹²⁴⁵ 57.76	⁰¹² 57.30	⁰¹² 57.44
D	¹ 50.75	49.88	¹ 50.63	01245 51.54	⁰¹² 51.33	⁰¹² 51.20
Е	¹ 49.70	49.23	⁰¹ 49.92	012 50.51	⁰¹² 50.52	⁰¹² 50.38
F	¹ 51.60	51.09	¹ 51.71	⁰¹² 52.28	⁰¹² 52.43	⁰¹² 52.32
G	¹ 49.50	49.06	⁰¹ 49.97	012 50.84	⁰¹² 50.88	⁰¹² 50.74
Н	¹ 49.77	49.50	⁰¹ 50.64	⁰¹² 51.16	⁰¹² 51.07	⁰¹² 51.10
average test	51.90	51.42	52.06	52.90	52.84	52.79
model size	366,869.4	448,359	1,478,049	100,000	100,000	100,000

- Multi-task tuning improves BLEU over all single-task runs.
- Also more efficient due to iterative feature selection.
- Difference between natural and random tasks inconclusive.

Single- and Multi-Task Margin Perceptron

	single-task tuning			n	nulti-task tuni	ing
	indep. ⁰	pooled 1	pooled-cat ²	IPC ³	sharding 4	resharding 5
pooled test	-	51.33	¹ 52.58	¹² 52.98	¹² 52.95	¹² 52.99
А	¹ 56.09	55.33	¹ 55.92	0124556.78	012 56.62	⁰¹² 56.53
В	¹ 52.45	51.59	¹ 52.44	⁰¹² 53.31	⁰¹² 53.35	⁰¹² 53.21
С	¹ 57.20	56.85	⁰¹ 57.54	⁰¹ 57.46	¹ 57.42	¹ 57.43
D	¹ 50.51	50.18	⁰¹ 51.38	⁰¹²⁴⁵ 52.14	0125 51.82	⁰¹² 51.66
Е	¹ 50.27	49.36	⁰¹ 50.72	⁰¹²⁴ 51.13	⁰¹² 50.89	⁰¹² 51.02
F	¹ 52.06	51.20	⁰¹ 52.61	⁰¹²⁴⁵ 53.07	⁰¹² 52.80	⁰¹² 52.87
G	¹ 50.00	49.58	⁰¹ 50.90	⁰¹²⁴⁵ 51.36	⁰¹² 51.19	⁰¹² 51.11
Н	¹ 50.57	49.80	⁰¹ 51.32	⁰¹² 51.57	⁰¹² 51.62	⁰¹ 51.47
average test	52.39	51.74	52.85	53.35	53.21	53.16
model size	423,731.5	484,483	1,697,398	100,000	100,000	100,000

- Single-task runs beat standard perceptron w/ and w/o ℓ_1 .
- Regularization by margin and multi-task learning adds up.
- Best result is nearly 2 BLEU points better than MERT.

			Conclusion
Conclusio	n		

- Multi-task learning for SMT is **efficient** due to online learning, parallelization and feature selection,
- but also effective in terms of BLEU improvements over single-task learning.
- Multi-task learning is **adaptive** due to path-following in regularization.
- Question: Can task definition be adapted to problem as well?
 - *Natural* task definition show nominal (not statistically significant) advantage.
 - Future work: Optimize clustering of IPC subclasses for multi-task learning in SMT.

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		Conclusion

IPC

IPC: 8 sections, 120 classes, 600 subclasses, 70,000 subgroups: Is there a *natural* or *useful* task definition for multi-task SMT?

		Conclusion

Code

 dtrain code is part of cdec: https://github.com/redpony/cdec. Introduction Algorithms Random Sharding Natural Tasks Conclusion

Thanks for your attention!

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